

An Internet Based Anonymous Electronic Cash System

Israt Jahan¹, Mohammad Zahidur Rahman², K M Akkas Ali³, Israt Jerin⁴

^{1,2}Department of Computer Science and Engineering, Jahangirnagar University, Dhaka, Bangladesh

³Institute of Information Technology, Jahangirnagar University, Dhaka, Bangladesh

⁴Britannia University, Paduar Bazar, Bissaw Road, Comilla, Bangladesh

ABSTRACT: There is an increase activity in research to improve the current electronic payment system which is parallel with the progress of internet. Electronic cash system is a cryptographic payment system which offers anonymity during withdrawal and purchase. Electronic cash displays serial numbers which can be recorded to allow further tracing. Contrary to their physical counterparts, e-cash have an inherent limitation; they are easy to copy and reuse (double-spending). An observer is a tamper-resistant device, issued by the Internet bank, which is incorporated with the Internet user's computer that prevents double-spending physically, i.e., the user has no access to her e-cash and therefore he cannot copy them. In this paper, we shall present an anonymous electronic cash scheme on the internet which incorporates tamper-resistant device with user-module.

KEYWORDS- E-cash, Double-spending, Tamper-resistant device, Blind signature, Internet banking.

I. INTRODUCTION

Electronic commerce is one of the most important applications for the internet. The prerequisite for establishing an electronic marketplace is a secure payment. Several electronic protocols have been proposed to implement different kinds of payment: credit card payments, micropayments, and digital e-cash. Cryptographically, the most challenging task is the design of digital e-cash for every payment system mentioned above we have the requirement that the payment token has to be unforgeable. In 1982, D. Chaum [7] presented the notion of blind signatures that offer the possibility to design electronic e-cash. The bank signs a set of data chosen by the user which guarantees both the unforgeability of the e-cash and their anonymity, since the bank does not get any information about data it signed. But blind signatures solve only half of the problem: since digital data can be copied, a user can spend a valid e-cash several times (double-spending) if the deposit of e-cash is not done on-line [3]. To validate each e-cash on-line means that the vendor has to contact the bank in every purchase. From the efficiency's point of view this is undesirable. Therefore, we restrict our attention to off-line systems, i.e., the vendor has to check the validity of e-cash without contacting the bank. An e-cash is constructed in a way that allows its owner to spend it anonymously once, but reveals his identification if he spent it twice [5]. From a theoretic point of view this solution is quite elegant. But in practice it is unsatisfactory. A way to prevent the user physically from copying her coins is to store essential parts of a coin in a tamper-resistant device called the observer [7].

II. AN E-CASH MODEL WITH TAMPER-RESISTANT DEVICE

An internet based anonymous off-line electronic e-cash scheme [1, 8 and 9] with tamper-resistant device consists of three collections of probabilistic, polynomially-bounded parties [2], a bank B, users U_i , and shops S_j , and four main procedures: withdrawal, blind signature issuing, payment and deposit (Figure 1). Users and shops maintain separate account with the Internet Bank [10].

- When user (U_i) needs e-cash, then Bank issues e-cash from user's account in his (user's) tamper-resistant device T_i over an authenticated channel.
- When user (U_i) wants to spend this e-cash, it is validated by bank (B) by blind signature issuing protocol.
- U_i spends an e-cash by participating in a payment protocol with a shop S_j over an anonymous channel, and
- S_j performs a deposit protocol with the bank B, to deposit the user's e-cash into his account.

- (1) Withdrawal protocol
- (2) Blind signature issuing protocol
- (3) Payment protocol
- (4) Deposit protocol

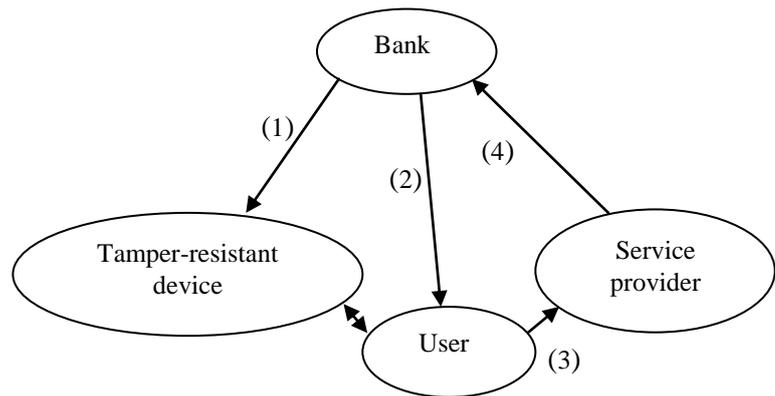


Figure 1: Model of e-cash with tamper-resistant device

III. AN INTERNET BASED ANONYMOUS E-CASH SYSTEM

We shall now represent an anonymous off-line e-cash transaction system on the Internet.

3.1 The Bank’s setup protocol

- All arithmetic is performed in a group G_q of prime order q chosen by bank (B). The bank generates independently at random four numbers $g_0, g_1, g_2, h \in G_q$ and a number $x \in Z_q$. The bank also determines a collision-free hash function $H(\cdot)$ such as to make the Schnorr signature scheme secure [4]. A public key that is issued by the bank to the user is a pair $(h'_i, a'_i) \in G_q * G_q$.
- The number x is the secret key of the bank, and the corresponding public key is the tuple $(g_0, g_1, g_2, h, G_q, H(\cdot))$. A certificate of the bank on the public key (h'_i, a'_i) of the user is a triple (z'_i, c', r) such that $c' = H(h'_i, a'_i, z'_i, g_0^{r'} h^{-c'})$.
- The secret key that corresponds to the public key (h'_i, a'_i) of the user is a pair $((\beta_1, \alpha_1), (\beta_2, \alpha_2))$, such that $h'_i = g_1^{\beta_1} g_2^{\alpha_1}$ and $a'_i = g_1^{\beta_2} g_2^{\alpha_2}$.

3.2 The actions

The Internet bank will be denoted by B, the user by U_i , and the service provider by S_j . The computer of U_i is denoted by C_i , and his tamper-resistant device by T_i .

3.2.1 Account establishment protocol

U_i installs on his computer, a software program for performing the protocols. When U_i opens an account with B, the following procedure takes place.

- C_i generates independently at random a secret key $x_{i2} \in Z_q$, and stores it. C_i sends $h_{i2} = g_1^{x_{i2}}$, to B, together with an appropriate verifiable description of the identity of U_i . It then generates independently at random a secret key $x_{i1} \in Z_q$ for U_i . B lists this number (h_{i2}) in its so-called account database, together with at least a balance variable that keeps track of the amount of money that U_i has in its account with B, and the description of U_i 's identity.
- B then issues to U_i a tamper-resistant device T_i which has stored in non-volatile memory at least the following items: the numbers x_{i1} and g_1 , and a description of G_q ; code to perform its role in the protocols; and a counter variable, from now on denoted by *balce*, that keeps track of the amount of money that is held by U_i .
- B makes $h_{i1} = g_1^{x_{i1}}$, known to U_i ; this is the public key of T_i . B then computes $h_i = h_{i1} h_{i2}$ (the joint public key of T_i and U_i and stores h_i in his account database along with its other information on U_i). The bank B does not know the joint secret key, $(x_{i1} + x_{i2}) \bmod q$, of T_i and U_i .
- Finally, B computes $(h_i g_2)^x$, which will henceforth be denoted by z_i known to U_i .

3.2.2 Withdrawal protocol

The withdrawal of electronic cash appears as follows:

T_i is assumed to have in common with B a secret key k . This secret key, and a sequence number, seq , (which has been set to some initial value, such as zero), have been stored by B before issuing T_i to U_i . In addition, the description of a one-way function $f_1(.)$ has been stored by B in T_i . B decreases the balance, $balce'$, of U_i by amount. It then increases seq by one, and transfers $v \leftarrow f_1(k, seq, amount)$ to T_i by sending it to C_i . T_i receives v from C_i . It then computes $f_1(k, seq, amount)$, and compares it for equality with v . If equality holds, it increases seq by one, and balance by amount.

The withdrawal protocol appears as follows:

Tamper-resistant Device (T_i)		Bank (B)
		$balce' \leftarrow balce' - amount$
Verify	$\leftarrow (v)-----$	$v \leftarrow f_1(k, seq, amount)$
$v = f_1(k, seq, amount)$		$seq \leftarrow seq + 1$
then, $seq \leftarrow seq + 1$		
$balce \leftarrow balce + amount$		

Table 1: The withdrawal protocol

3.2.3 The Pre-processing of blind signature issuing protocol

Payment of an amount requires U_i to provide the service provider with a signature on the amount (and additional data). To prepare for the withdrawal of a blind signature on e-cash, T_i and C_i perform the following off-line processing.

- T_i generates independently at random a number $w_i \in_R Z_q$, and sends $a_i g_1^{w_i}$ to C_i . T_i stores w_i for later use in the payment protocol.
- C_i generates independently at random a vector $(\alpha_1, \alpha_2, \alpha_3, \alpha_4, \alpha_5) \in Z_q^5$, such that $\alpha_i \neq 0 \pmod q$. It then computes $h_i' \leftarrow (h_i g_2)^{\alpha_1}$, $a_i' = a_i^{\alpha_1} g_1^{\alpha_2} g_2^{\alpha_3}$, $z_i' \leftarrow z_i^{\alpha_1}$, $temp_1 = h_i^{\alpha_4} g_0^{\alpha_5}$, $temp_2 \leftarrow (z_i')^{\alpha_4} (h_i g_2)^{\alpha_1 \alpha_5}$.
- C_i stores (h_i', a_i') and $(\alpha_1, \alpha_2, \alpha_3)$ and $temp_1, temp_2, \alpha_4$ and α_5 for the later use in the payment protocol.

3.2.4 The blind signature issuing protocol

The issuing of blind signature [6] is done by means of the following on-line certificate issuing protocol between C_i and B. The blind signature issuing appears as follows:

Computer(C_i)		Bank(B)
		$w \in Z_q$
		$a \leftarrow g_0^w$
		$b \leftarrow (h_i g_2)^w$
	$\leftarrow (a,b)-----$	
$c' \leftarrow H(h_i', a_i', a temp_1, b^{\alpha_1} temp_2)$		
$c \leftarrow c' + \alpha_4 \pmod q$	$----- (c) \rightarrow$	
	$\leftarrow (r)-----$	$r \leftarrow cx + w \pmod q$

Table 2: The blind signature issuing protocol

3.2.5 The pre-processing of payment protocol

To pay to S_j an amount, T_i and C_i perform the following pre-processing.

- C_i determines the specification, denoted by $spec$, of the payment. This number is a concatenation, in a standardized format, of that is to be transferred, the time and date of transaction, and an identification number that is uniquely associated with S_j . Additional data fields may be included in variable $spec$. C_i then sends (h_i', a_i') and $spec$ to T_i .
- T_i verifies that w_i is still in memory, and that balance exceeds amount (T_i can read this value from $spec$). If this is the case, it computes $d = H(h_i', a_i', spec)$ and $r_1 = dx_{i1} + w_i \pmod q$. It then decreases balance by amount, erases w_i from memory, and sends r_1 to C_i .
- C_i computes $d = H(h_i', a_i', spec)$, and verifies that $g_1^{r_1} h_{i1}^{-d} = a_i$. If this is the case, C_i computes $r_1' = \alpha_1(r_1 + dx_{i2}) + \alpha_2 \pmod q$, $r_2 \leftarrow d\alpha_1 + \alpha_3 \pmod q$. The pre-processing of payment protocol appears as follows:

<p>User computer(C_i)</p> <p>----- (h_i' , a_i') →</p> <p>←(r₁)-----</p> <p>d=H(h_i' , a_i' ,spec)</p> <p>verify</p> <p>$g_1^{r_1} h_{i1}^{-d} = a_i$</p> <p>$r_1' \leftarrow \alpha_1(r_1 + dx_{i2}) + \alpha_2 \text{ mod } q$</p> <p>$r_2 \leftarrow d\alpha_1 + \alpha_3 \text{ mod } q$</p>	<p>Tamper-resistant device(T_i)</p> <p>d=H(h_i' , a_i' ,spec)</p> <p>balce → balce - amount</p> <p>$r_1 = dx_{i1} + w_i$</p> <p>erases w_i</p>
---	--

Table 3: The preprocessing of payment protocol

3.2.6 The payment protocol

The actual payment is done by means of the following on-line payment protocol between C_i and S_j.

- C_i sends (h_i' , a_i'),(z_i' ,c' ,r'),(r₁' ,r₂')to S_j.
- S_j computers d in the same way as did C_i and T_i and accepts the transferred information if and only if $h_i' \neq 1$, $c' = H(h_i' , a_i' , z_i' , g_o^r h^{-c'} , (h_i')^{r'} (z_i')^{-c'})$ and $g_1^{r_1'} g_2^{r_2'} (h_i')^{-d} = a_i'$
- The payment protocol appears as follows:

<p>Computer(C_i)</p> <p>-- (h_i' , a_i'),(z_i' ,c' ,r'),(r₁' ,r₂') →</p>	<p>Service Provider(S_j)</p> <p>Check</p> <p>d=H(h_i' , a_i' ,spec)</p> <p>$c' = H(h_i' , a_i' , z_i' , g_o^r h^{-c'} , (h_i')^{r'} (z_i')^{-c'})$</p> <p>$g_1^{r_1'} g_2^{r_2'} (h_i')^{-d} = a_i'$</p>
--	---

Table 4: The payment protocol

3.2.7 The deposit Protocol

At a suitable time, preferably when network traffic is low, S_j sends the payment transcript, consisting of (h_i' ,a_i'), (z_i' , c' , r'), (r₁' ,r₂') and spec, to B.

B verifies that spec has been formed correctly by S_j. If this is the case, it searches its so-called deposit database to find out if it has stored (h_i' ,a_i') before.

There are two possible situations:

1. (h_i' ,a_i') is not in the deposit database. B then computes $d = H(h_i' , a_i' , spec)$, and verifies the payment transcript by verifying that $h_i' \neq 1$, $c' = H(h_i' , a_i' , z_i' , g_o^r h^{-c'} , (h_i')^{r'} (z_i')^{-c'})$ and $g_1^{r_1'} g_2^{r_2'} (h_i')^{-d} = a_i'$. If these verifications hold, B stores (h_i' , a_i'),(z_i' ,c' ,r') and (r₁' ,r₂') in the deposit database, and credits the account of S_j by amount.
2. (h_i' ,a_i') is already in the deposit database. In that case a fraud has occurred. If spec of the already stored information is identical to that of the new payment transcript, then S_j is trying to deposit the same transcript twice.

Otherwise, B verifies the transcript as described insituation 1. If the verification holds (the payment transcript is valid), then the certified public key (h_i' ,a_i') must have been double-spent with overwhelming probability. Since, B now has at its disposal a pair (r₁' ,r₂') from the new transcript and a pair, say (r₁'',r₂''), from the already deposited information, it can compute $(r_1' - r_1'') / (r_2' - r_2'') \text{ mod } q$. B then searches its account database for joint public key $g_1^{(r_1' - r_1'') / (r_2' - r_2'')}$. Since, the identity of the corresponding account holder is known to B, appropriate legal actions can be taken. The number $(r_1' - r_1'') / (r_2' - r_2'') \text{ mod } q$ serves as the proof of B that the traced user has compromised his tamper-resistant device and has double-spent the certified public key (h_i' ,a_i') .

IV. DISCUSSIONS

In the e-cash scheme with tamper-resistant device, the user's secret is shared between the user and his observer. The combined secret is a modular sum of the two shares, so one share of the secret reveals no information about the combined secret. Co-operation of the user and the tamper-resistant device is necessary in order to create a valid response to a challenge during a payment transaction. It prevents the tamper resistant device from leaking any information about the user.

V. CONCLUSIONS

We presented electronic cash system which provides a physical defense against double-spending detection. To guarantee the prevention of double-spending, the bank has to be sure that the tamper-resistant device cannot be tampered with by the users. The use of a tamper-resistant device is a kind of first line of defense. If the user cannot manipulate the device, the tamper-resistant device can prevent double-spending. If the user succeeds in tampering the observer, the double-spending detection identifies the user afterwards.

REFERENCES

- [1] Ogiela, M.R., & Sulkowski, P. Improved Cryptographic protocol for digital coin exchange. *15th International Symposium on Soft Computing and Intelligent Systems (SCIS)*, 2014, 1148-1151.
- [2] Miers, I., Garman, C., Green, M., & Rubin, A.D. Zerocoin: Anonymous Distributed E-Cash from Bitcoin. *IEEE Symposium on Security and Privacy (SP)*, 2013, 397-411.
- [3] Jiangxiao Zhang., Zhoujun Li., Hua Guo., & Chang Xu. Efficient Divisible E-Cash in the Standard Model. *IEEE International Conference on Green Computing and Communications (GreenCom)*, 2013, 2123-2128.
- [4] Yun-kyung Lee., Seung-Wan Han., Sok-joon Lee., Byung-ho Chung., & Deok Gyu Lee. Anonymous Authentication System Using Group Signature. *International Conference on Complex, Intelligent and Software Intensive Systems*, 2009, 1235-1239.
- [5] Israt Jahan., Mohammad Zahidur Rahman., & Md. Golam Moazzem. Review of Anonymous Electronic Payment System. *Journal of Electronics and Computer Science*, 2003, 25-39.
- [6] Tsiounis, Y.S. Efficient Electronic Cash: New Notions and Techniques. *Northern University, Massachusetts*. PhD Thesis, 1997.
- [7] Chaum, D., & Pedersen, T. Wallet Databases with Observers. *In proceedings of CRYPTO*, 1993, 89-105.
- [8] Brands, S. Untraceable Off-line Cash in Wallets With Observers. *In proceedings of CRYPTO*, 1993, 303-318.
- [9] Schnorr, C.P. Efficient Signature Generation by Smart Cards. *Journal of Cryptology*, 1991, 4(3), 161-174.
- [10] Chaum, D. Blind Signatures for Untraceable Payments. *Advances in cryptology-Proceedings of Crypto '82, Lecture Notes in Computer Science*. Springer-Verlag, 1982, 199-203.